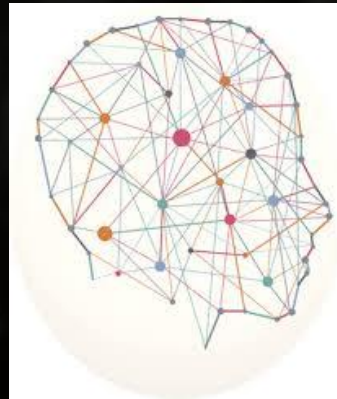


# Complexity in financial markets

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ESSEC course “ Managing in complexity ”

Chaire ESSEC Edgar Morin de la complexité



Wednesday 4<sup>th</sup> May 2016 - ESSEC

# Complexity in financial markets

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- Themes of the talk:
  - Feeling complexity in financial markets with SimTrade
    - From simplicity to complexity
  - Complexity / Risk and uncertainty
  - Complexity / Crisis
    - Statistical approach: extreme value theory
    - Historical approach: lessons from history to understand the process of financial crises

# Risk and uncertainty

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- Frank Knight (1885 - 1972)
- Professor of economics at the University of Chicago
- Cofounder of the Chicago School
- Author of the book « Risk, uncertainty and profit » published in 1921 (a reference)

# A business point of view (1)

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- « Business as usual »
  - Exemple: a groceryshop at the corner of the street
  - Economic theory says: in a competitive environment, at equilibrium, the firm (managers / shareholders) does not make any profit (no economic profit but accounting profit).
  - The remuneration of the firm is linked to the risk taken by the firm.
  - « Just make money » (usual return)

# A business point of view (2)

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- « Innovative business »
  - Example : start-up
  - Knight says: the firm (the entrepreneur) can make a profit (economic profit).
  - « Make a fortune » (abnormal return)

# Risk and uncertainty (1)

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- Risk
  - A probability can be associated to each event.
    - Calculable risk (theoretical model)
      - Example: a perfect dice
    - Estimable risk (data and a statistical model)
      - Example: an imperfect dice that you have launched  $n$  times.

# Risk and uncertainty (2)

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- Uncertainty
  - A probability cannot be associated to events.
    - No theory
    - No data
      - Example: an imperfect dice that you have never launched.

# Risk and uncertainty (3)

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- Open questions
  - In finance: risk or uncertainty?
  - In ther fields?

# Business, risk and uncertainty

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- Knight says:
  - « Business as usual » : risk
  - « Innovative business » : uncertainty
- Impact in terms of financing
  - Risk → Credit
  - Uncertainty → Capital

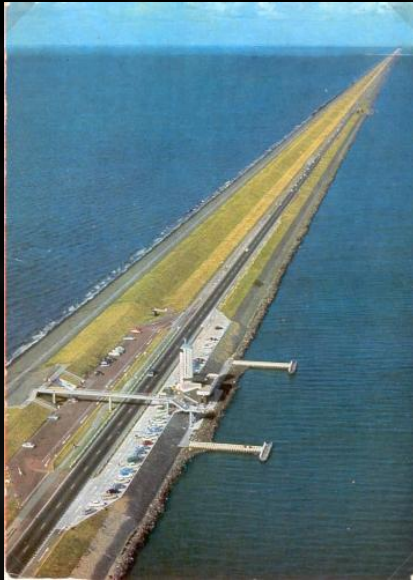
# Extreme events in finance

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- A statistical tool: extreme value theory (EVT)
  - Definition of an extreme event (from a statistical point of view)
  - Presentation of results
  - Applications in finance

# Uses of extreme value theory

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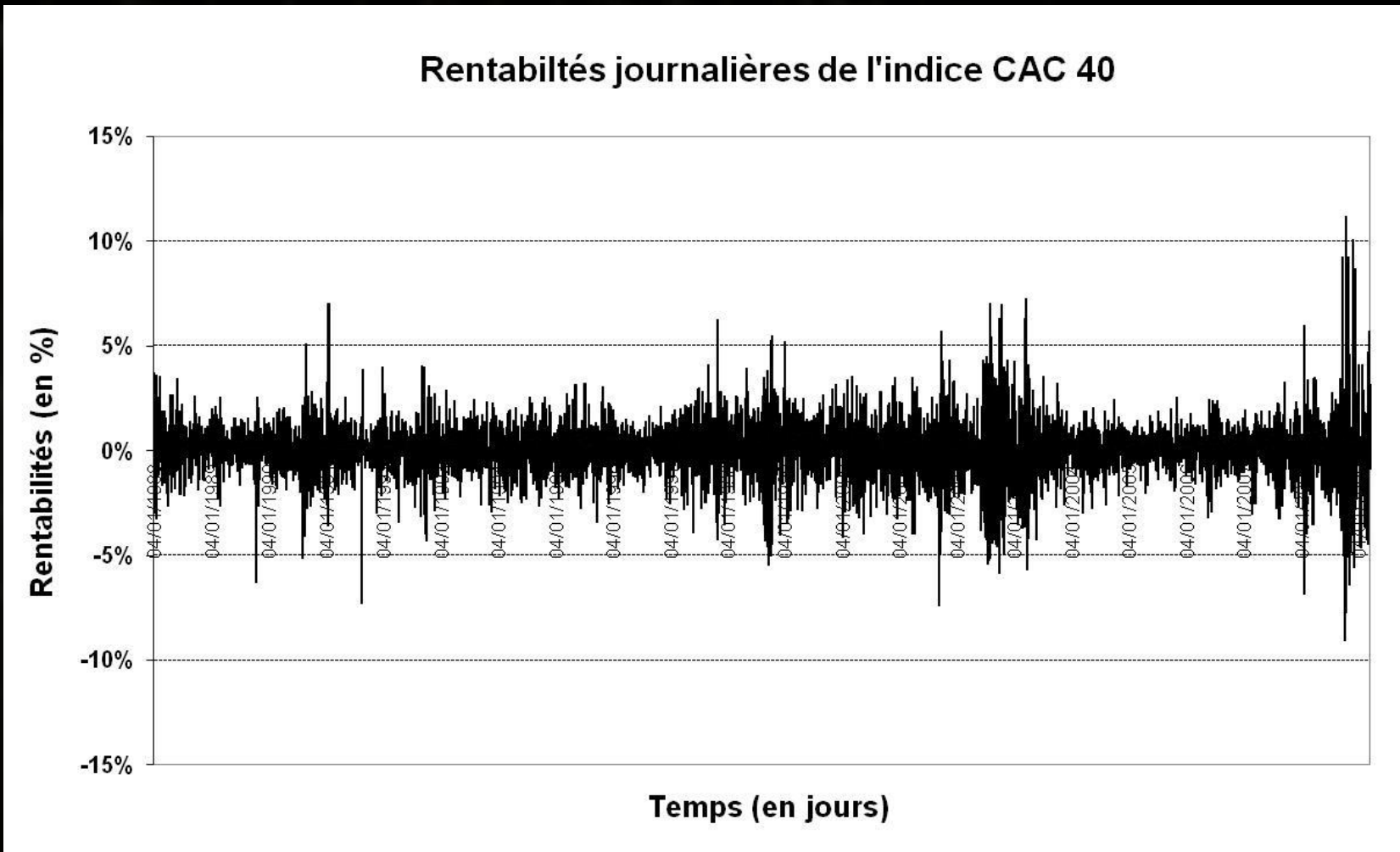


# Variable that is studied in finance

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- A random variable :
  - Variation of the value of a market position (trading room)
  - Variation of the value of a portfolio (asset management)
  - Return of a financial product

# Example: return on the CAC 40 index

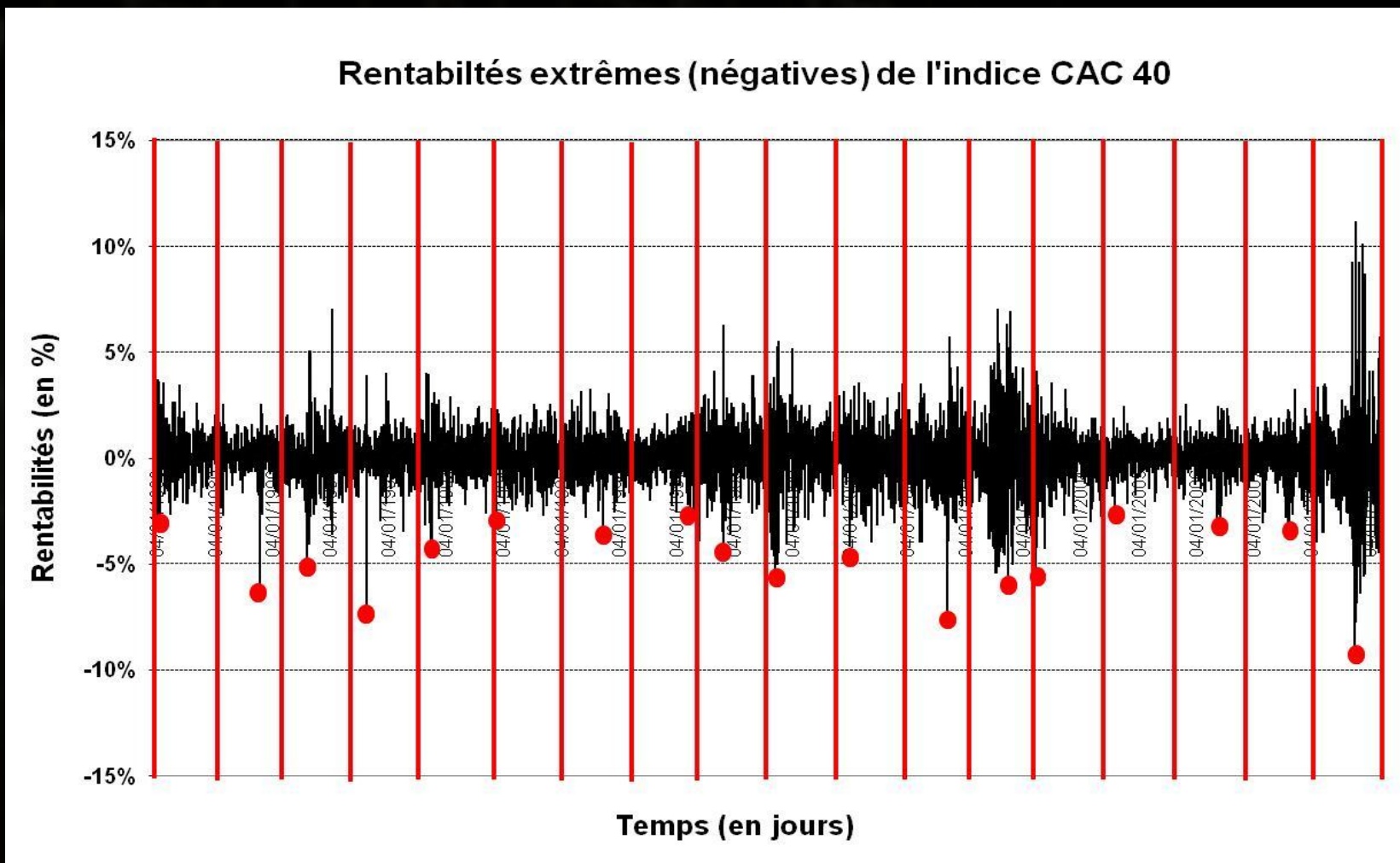


# Extreme events

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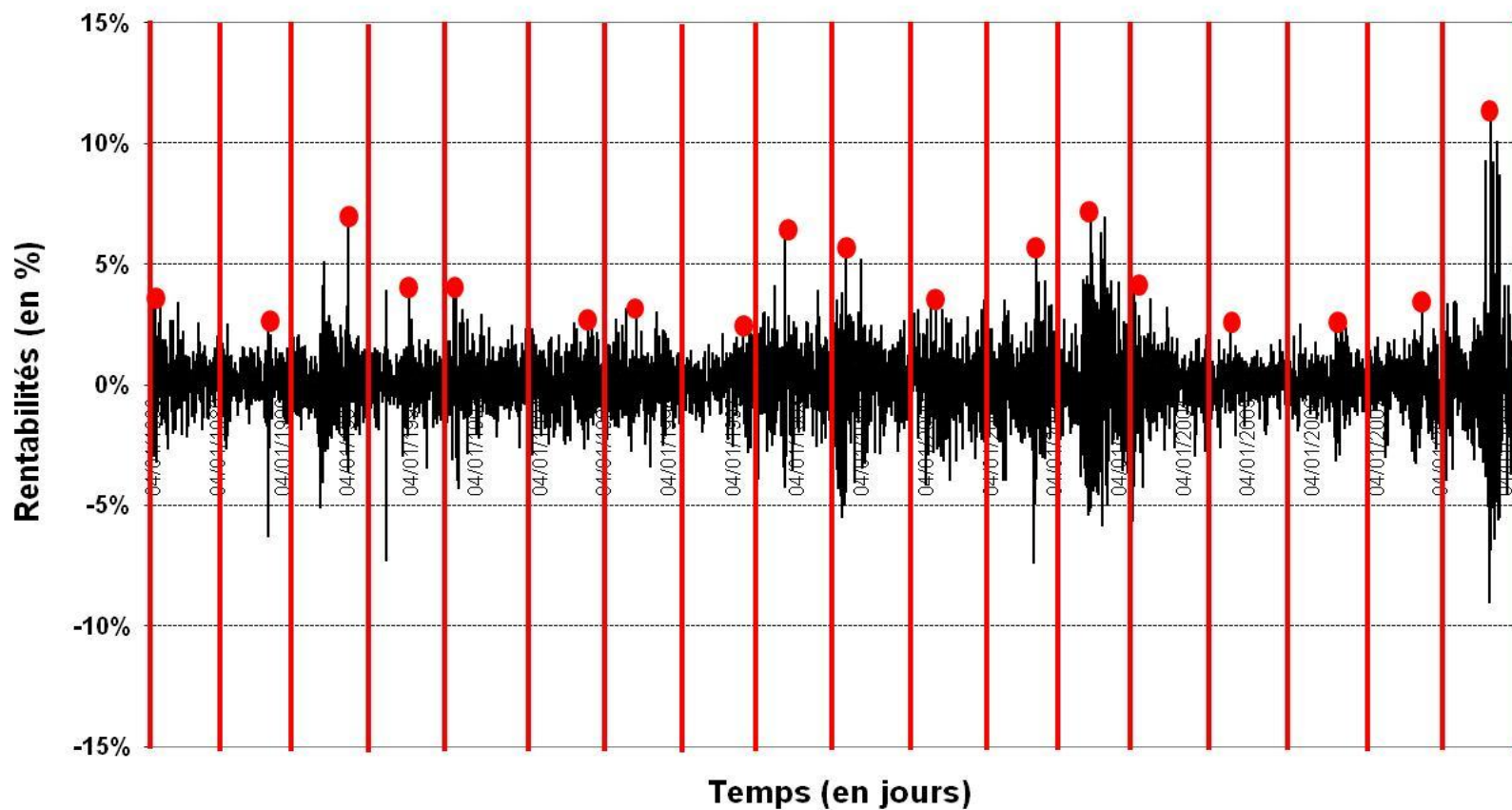
- EVT is interested in extreme observations:
  - The minimum (the lowest observation over a given time-period)
  - The maximum (the largest observation)

# Example: minimal return on the CAC 40 index (1)



# Example: maximal return on the CAC 40 index (2)

Rentabilités extrêmes (positives) de l'indice CAC 40



# Extreme value theory (1)

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- Statistical theory (1920-1940) which studies the limit distribution (when the number of observations tends to infinity)
- Theoretical result:
  - Existence of an asymptotic distribution
  - Three parameters :
    - Mean  $\mu$
    - Standard deviation  $\sigma$
    - Tail index  $\tau$

$$G_Y(y) = \exp\left(-\left(1 - \tau \cdot \frac{y - \mu}{\sigma}\right)^{\frac{1}{\tau}}\right)$$

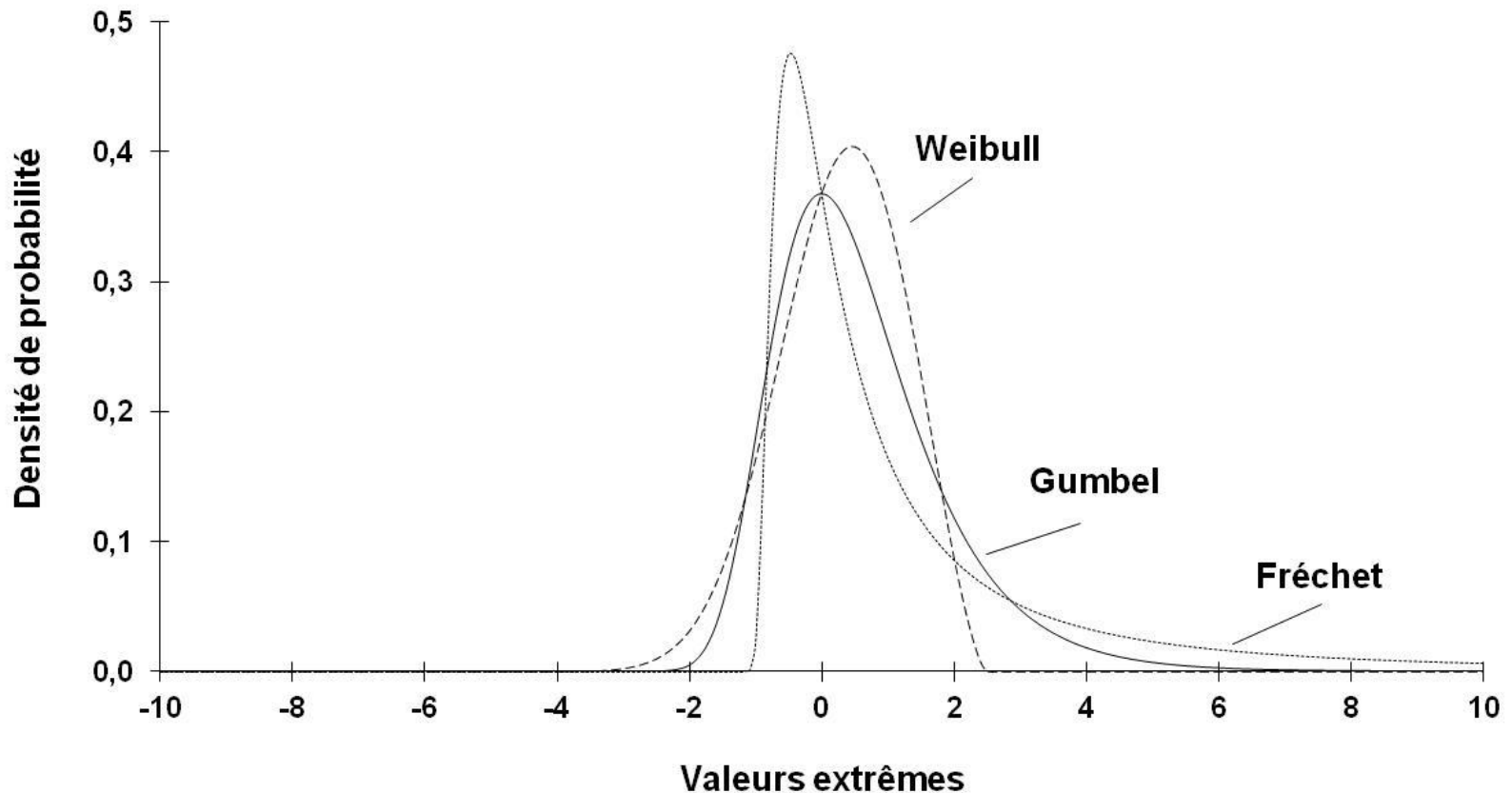
# Extreme value theory (2)

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- According to the tail index value:
  - $\tau < 0$ 
    - Weibull distribution
    - No tail
  - $\tau = 0$ 
    - Gumbel distribution
    - Thin tail
  - $\tau > 0$ 
    - Fréchet distribution
    - Fat tail

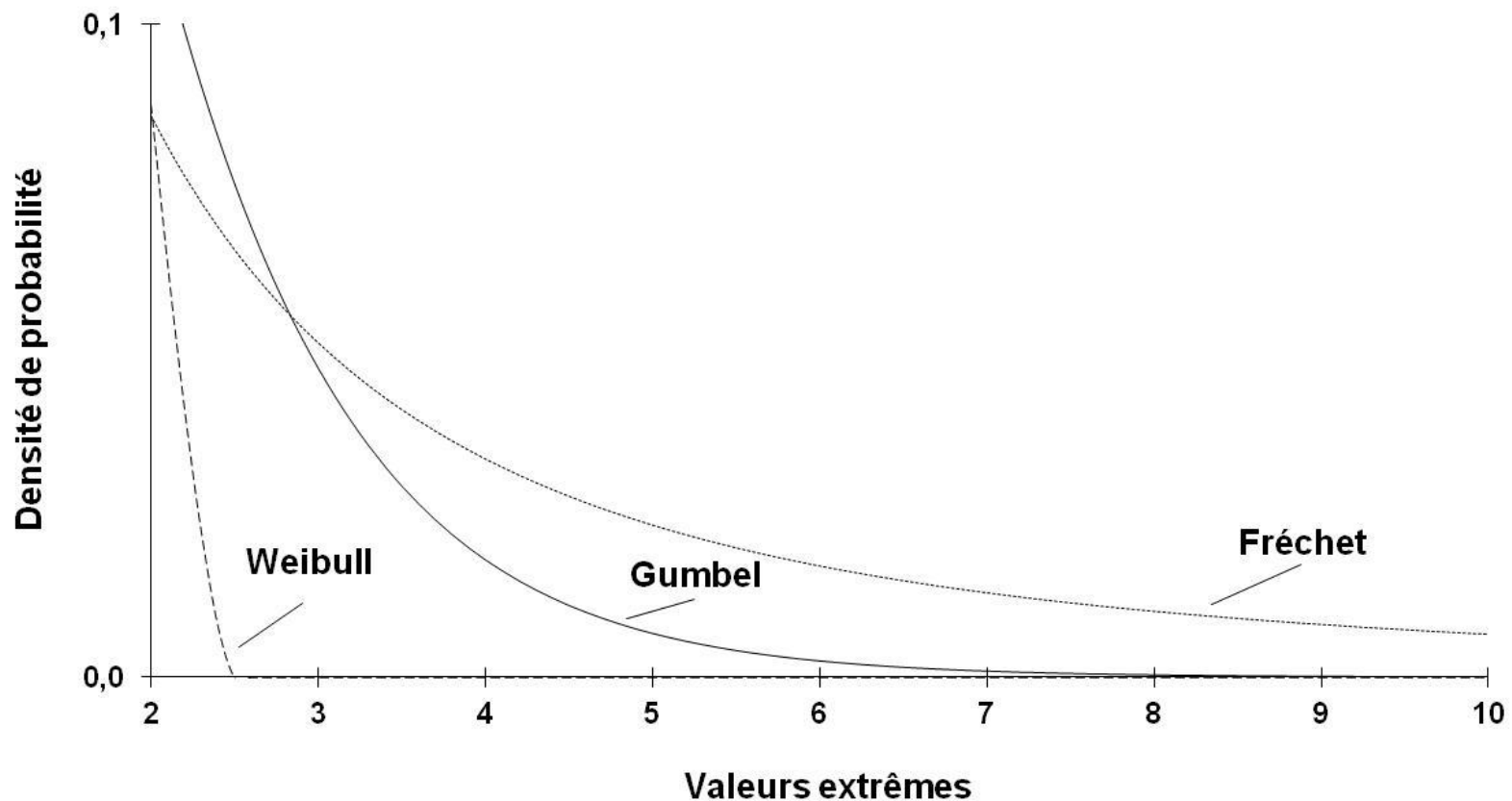
# Extreme value distributions

Lois d'extrêmes : Weibull, Gumbel et Fréchet



# Extreme value distributions: zoom on the tails

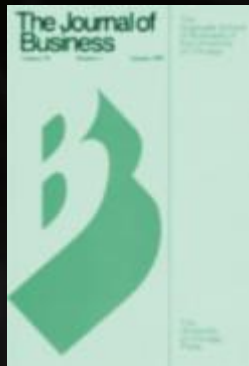
Lois d'extrêmes : Weibull, Gumbel et Fréchet



# Extremes in finance (1)

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- Empirical results: application of extreme value theory



Reference : Longin F. (1996) The asymptotic distribution of extreme stock market returns *Journal of Business*, N°63, pp 383-408.

# Extremes in finance (2)

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- Empirical results: a Fréchet distribution with a tail index between 0.1 and 0.4.
  - Similar results for individual stocks, stock indexes, interest rates, bond returns, foreign exchange rates, commodities, etc.
  - Similar results across time-periods
  - Similar results with different frequencies (daily, weekly, monthly)

# Extremes in finance (3)

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- A Fréchet distribution for extremes:  
stylized fact about financial asset prices
- Other stylized facts:
  - Bell curve for the distribution of returns
  - Week auto-correlation of returns
  - Week auto-correlation of squared returns  
(persistence of volatility)
  - Fat-tailed distributions

# Knight and extremes in finance: a paradox (1)

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- On the one hand:
  - Extreme events in finance (booms and crashes) are associated with periods of innovation.
    - Technical innovations during the internet bubble
    - Financial innovations during the subprime crisis
  - Extreme events in finance are associated with periods of great uncertainty.
  - Extreme events in finance are not well understood (« outliers »).

# Knight and extremes: a paradox(2)

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- On the other hand:
  - By application of extreme value theory, we know very well the statistical distribution of extreme returns even if we do not know precisely the statistical distribution of returns.
- Let's go back to Knight:
  - Difference between risk and uncertainty
  - Paradox
    - Extreme events : precise risk
    - Normal events : uncertainty / risk

# Applications of EVT in finance

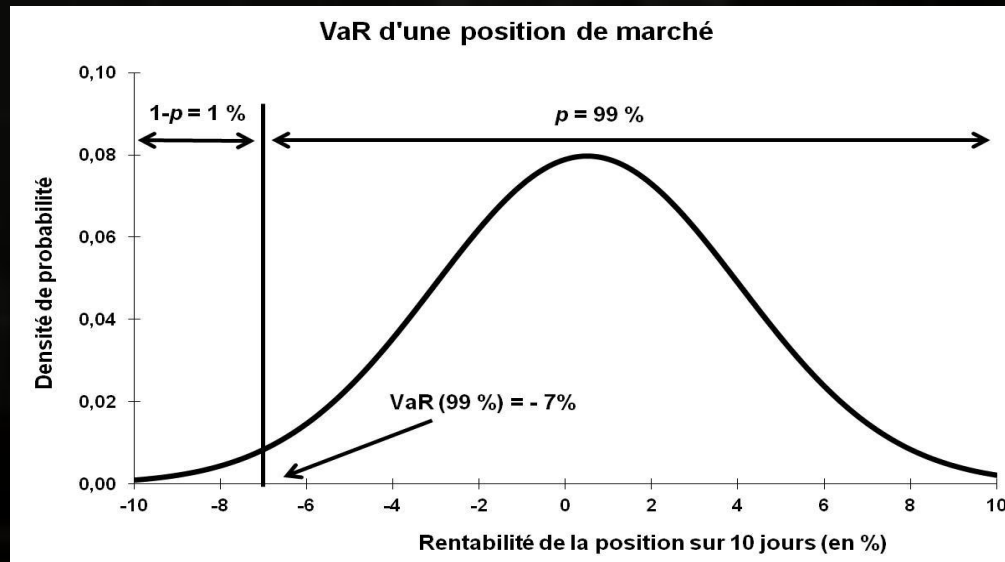
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- Risk management
  - VaR and stress testing of a market position
  - Setting of deposit in derivatives markets
- Portfolio management
  - Calibration of management methods for capital guaranteed products
- Financial modelling
  - Choice of the process for returns

# Value at risk and stress testing (1)

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- Value at risk (VaR) :
  - Loss of a market position over a given time-period  $T$  for a given probability level  $p$  donnée
  - Example: 10 day 99% VaR



# Value at risk and stress testing (2)

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- Computation of VaR in practice
  - Choice of method: variance-covariance (normal distribution), historical, Monte Carlo
- VaR corresponds to ordinary market conditions
  - Waiting-time period (average time that we have to wait) for 10 day 99% VaR: 4 years

# Value at risk and stress testing (3)

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- 4 years: quite short!
- Necessity to have a model to complete VaR model : stress testing (useful for internal management / regulatory requests to validate internal models)
- Stress testing corresponds to extraordinary market conditions
  - Waiting-time period: 20 years, 50 years (in finance) 200 years in insurance

# Value at risk and stress testing (4)

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- Models used to compute VaR (mainly based on the thin-tailed normal distribution) cannot be used for stress testing.
- Utility of extreme value theory to model distribution tails properly

# Ad !

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# Beyond numbers... stories

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- Historical approach
  - Work by historians on financial crises (Zola, Aftalion, Galbraith)
  - Formalization by Kindleberger « *Manias, Panics, and Crashes: A History of Financial Crises* »
    - Anatomy of bubbles and financial crises

# Anatomy of a financial crisis

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- Kindleberger (Minsky) distinguishes five stages:
  - Change
  - Boom
  - Euphoria
  - Crisis
  - Revulsion

# Anatomy of a financial crisis (1)

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- Stage 1 : Change / shock / *Displacement*
  - Apparition of a new element (technological innovation, regulatory change, political event)
  - Crisis of 2007: political will to make American people own their home, period of low interest rates, financial innovation (structured products in the credit market)

# Anatomy of a financial crisis (2)

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- Stage 2: Boom
  - The phenomenon is rather limited to professionals.
  - Increase in prices
  - Importance of credit
    - At the economic level (firms)
    - At the financial level (investors)

# Anatomy of a financial crisis (3)

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- Stage 3 : Euphoria
  - The general public (individual investors) is affected by the phenomon.
  - Sharp increase in prices (exponential)
  - Difficulty to liquidate positions
  - Positive contributions from the media

# Anatomy of a financial crisis (4)

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- Stage 4 : Crisis
  - Sell by professionals and informed traders
  - Triggering event
  - Panics sales by speculators and individuals
  - Lack of liquidity

# Anatomy of a financial crisis (5)

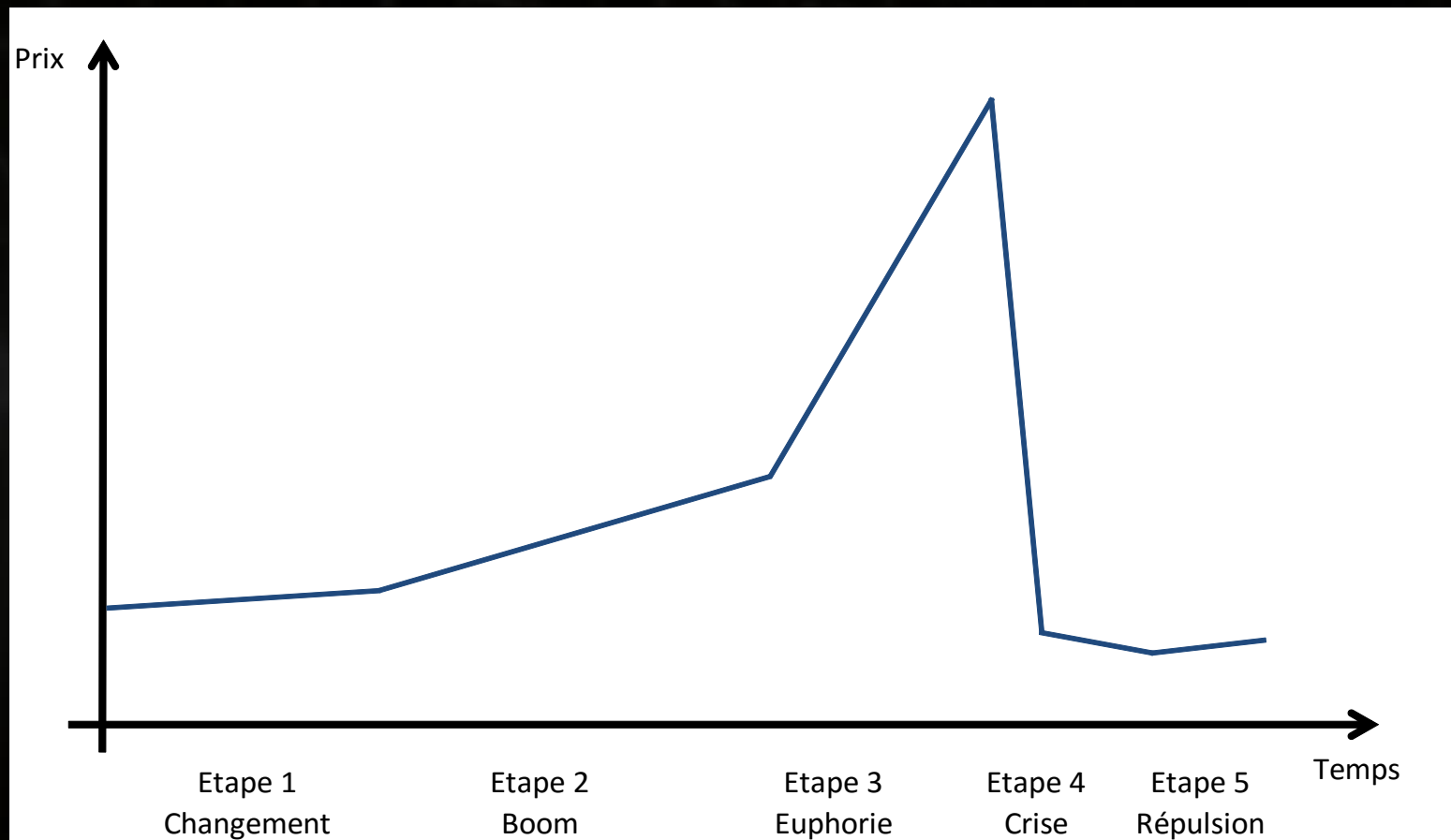
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- Stage 5 : Revulsion
  - Negative contributions from the media (fraud stories)
  - Search for culprits
  - Lender of last resort

# Anatomy of a financial crisis

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- Price process



# Conclusion

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- Crises : rare, extreme, extraordinary particular events
- Message : **regularity in the phenomenon**
  - Approach by statisticians: these events obey to a well-known distribution : the Fréchet distribution (robust result)
  - Approach by historians: we always observe the same pattern for these events

# A third approach: simulations

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- Developp a new approach based on simulations for a deep undestanding of the phenomena (bubbles and crashes)

The logo for SimTrade, featuring a stylized orange 'S' followed by the text 'imTrade' in a dark blue, sans-serif font.

- Available on [www.simtrade.fr](http://www.simtrade.fr)
- Concept of simulation

# A few citations by Edgar Morin

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- « Toute connaissance (et conscience) qui ne peut concevoir l'individualité, la subjectivité, qui ne peut inclure l'observateur dans son observation, est infirme pour penser tous problèmes, surtout les problèmes éthiques. »
- « La connaissance est une navigation dans un océan d'incertitudes à travers des archipels de certitudes. »
- « Rétrospectivement, tout semble logique mais quand on le vit au fur et à mesure, tout arrive de façon imprévue. »

# SimTrade

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What is SimTrade?

What are the objectives of SimTrade?

What is the originality of SimTrade?

# SimTrade: 3 key points

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- SimTrade: pedagogical tool in finance
- Objective of SimTrade: pedagogical
  - ▶ To understand financial markets
  - ▶ To learn to act in financial markets
- Originality of SimTrade
  - ▶ Complete simulation: markets and firms
  - ▶ Advantage: impact of SimTrader on the market

# SimTrade: a story in 3 words


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- Learn
  - Courses
- Learn by trading
  - Simulations
- Compete
  - Competitions



# SimTrade demo

FORMATIONS SIMULATIONS CONCOURS CERTIFICATS *SimTrade* SE CONNECTER






### Formations

Apprendre la finance de marchés et la finance d'entreprise avec les formations SimTrade.


Apprendre



### Simulations

Pratiquer les marchés avec la plate-forme de simulations de trading SimTrade.


Pratiquer



### Concours

Participer aux concours et duels de trading pour confronter ses stratégies boursières.

Participer



### Certificats

Valider ses connaissances et compétences avec les certificats SimTrade.

Valider

**Passez un ordre de Bourse et influencez le marché !**

En moins de 10 minutes, suivez votre premier cours pour comprendre le fonctionnement du marché puis lancez votre première simulation SimTrade pour passer un ordre et influencer le marché.

[Suivre le cours](#) [Lancer la simulation](#)

### Blog SimTrade

- SimTrade : MOOC sur les marchés financiers
- Approche pédagogique de SimTrade (Partie 1) : la liberté d'apprendre
- Approche pédagogique de SimTrade (Partie 2) : objectifs d'apprentissage et évaluation

# Complexity of financial markets (1)

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- Modeling of the market

Market: place where buyers and sellers meet  
(traders/ investors in financial markets)

Modeling of traders :

→ Motivation / objective: liquidity, information, etc.

→ Strategies

→ Orders (characteristics)

→ Trading platform (infrastructure de marché)

→ Transactions (price and volume)

# Complexity of financial markets (2)

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- Tool to simulate random numbers

Monte Carlo method

Series of numbers  $U_n$  between 0 and  $m$

First number :  $U_1$  (seed of simulation)

Example :  $U_1 = 10$

Generation of next random numbers :

$$U_{n+1} = a \times U_n + b \pmod{m}$$

Example :  $a = 23$ ,  $b = 3$  et  $m = 100$

See the Excel file

# Complexity of financial markets (3)

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- Use of random numbers

Simulation of the behavior of simulated traders

Active or inactive ?

If active : buy or sell? (direction of the order)

Other characteristics of the order:

Type

Quantity or amount

Date of validation

# Complexity of financial markets (4)

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- Randomness of the simulation
  - ▶ Simulations which can be reproduced identically at every launch: randomness will come from the SimTrader (impact on the market)
  - ▶ Simulations which cannot be reproduced identically at every launch: randomness will come from the seed
  - ▶ Simulations which cannot be reproduced identically at every launch: randomness will come from the events (news flow)

# Illustration of complexity in financial markets

Change in the seed of the simulation algo

Seed = 122

Seed = 123

Seed = 124



# Work by Edgar Morin

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- La pensée complexe
  - « Pense-bête » : never forget that the world is complex

# Continuation of my work (1)

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- SimTrade :
  - Research side (experimental economics / experimental finance) :
    - Use of simulations by SimTraders
    - To understand the behavior of investors
    - To explain stylized facts in financial markets

# Continuation of my work (2)

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- Simulation Tulipmania



# Conclusion (1)

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- Different approaches
  - Mathematical model
    - Statistical methods to model risk
    - Model of risk / Risk model (uncertainty)
    - Paradox in times of crisis
  - History
    - History seems to repeat itself
  - Simulation
    - Complexity and risk
    - Interactions between agents (role of expectations)

# Conclusion (2)

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Citation of Alan Greenspan (Fed)

“I guess I should warn you,  
if I turn out to be particularly clear,  
you've probably misunderstood  
what I've said.”

« Si vous m'avez compris,  
c'est sans doute que je me suis  
mal expliqué. »